



# Implementation of Scientific Computing Applications on the Cell Broadband Engine processor

*Guochun Shi,  
Volodymyr Kindratenko*



National Center for Supercomputing Applications  
University of Illinois at Urbana-Champaign

# Three scientific applications

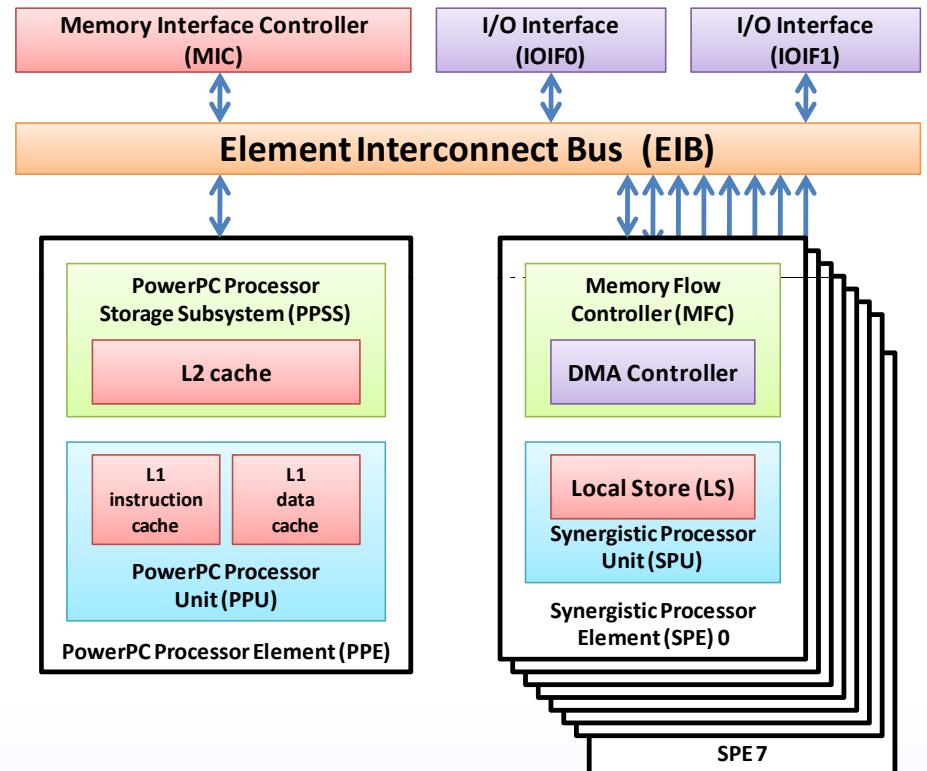
- Nanoscale Molecule Dynamics (NAMD)
  - James Philips from Theoretical and Computation Biophysics group, UIUC
- MIMD Lattice Computation (MILC)
  - Steven Gottlieb from physics department, Indiana University
- Electron Repulsion Integral (ERI) in quantum chemistry
  - Ivan S. Ufimtsev, Todd J. Martinez, Chemistry department, UIUC

# Presentation outline

- Introduction
  - Cell Broadband Engine
  - Target Applications
    1. NAnoscale Molecule Dynamics (NAMD)
    2. MIMD Lattice Computation (MILC) collaboration
    3. Electron Repulsion Integral (ERI) in quantum chemistry
  - In-house task library and task dispatch system
- Implementation and performance
  - Application porting and optimization
- Summary
- Conclusions

# Cell Broadband Engine

- One Power Processor Element (PPE) and eight Synergistic Processing Elements (SPE), each SPE has 256 KB local storage
- 3.2 GHz processor
- 25.6 GB/s processor-to-memory bandwidth
- > 200 GB/s EIB sustained aggregate bandwidth
- Theoretical peak performance of 204.8 GFLOPS (SP) and 14.63 GFLOPS (DP)



# In-house task library and dispatch system

## Compute task struct

```
typedef struct task_s {  
    int cmd; // operand  
    int size; // the size of task structure  
} task_t;
```

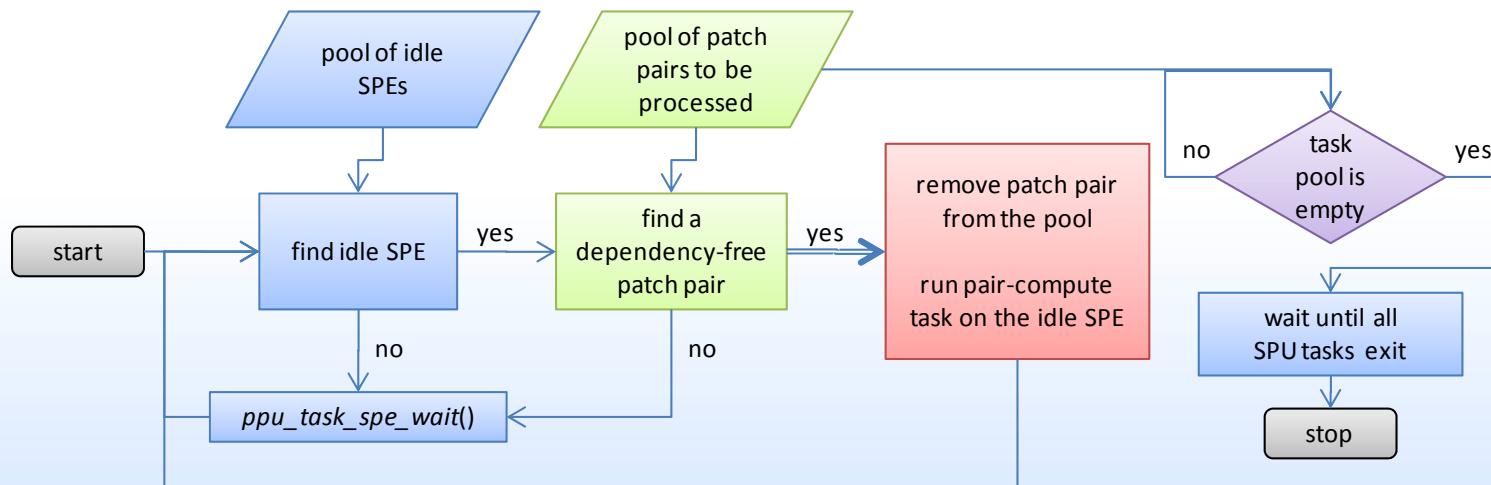
```
typedef struct compute_task_s {  
    task_t common;  
    <user_type1> <user_var_name1>  
    <user_type2> <user_var_name2>  
    ...  
} compute_task_t;
```

## API for PPE and SPE

```
int ppu_task_init(int argc, char **argv,spe_program_handle_t ); // initialization  
int ppu_task_run(volatile task_t * task); // start a task in all SPEs  
int ppu_task_spu_run(volatile task_t * task, int spe); // start a task in one SPE  
int ppu_task_spu_wait(void); // wait for any SPE to finish, blocking call  
void ppu_task_spu_waitall(void); // wait for all SPEs to finish, blocking all
```

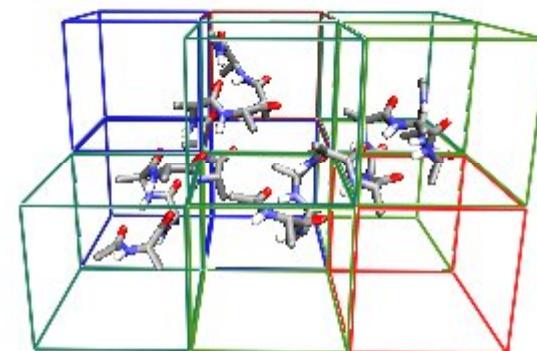
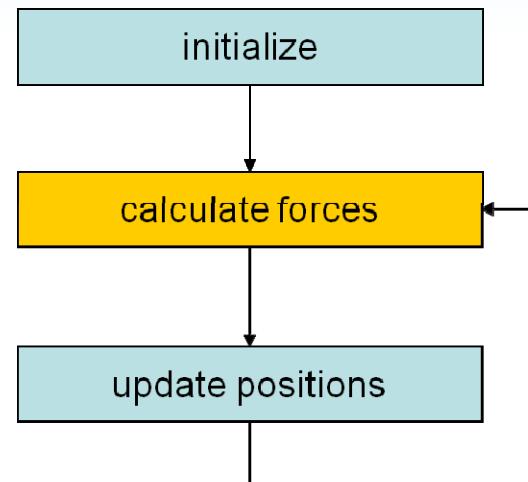
```
int spu_task_init(unsigned long long);  
int spu_task_register(dotask_t,int); // register a task  
int spu_task_run(void); // start the infinite loop, wait for tasks
```

## Task dispatch system in NAMD



# NAMD

- Compute forces and update positions repeatedly
- The simulation space is divided into rectangular regions called patches
  - Patch dimensions > cutoff radius for non-bonded interaction
- Each patch only needs to be checked against nearby patches
  - Self-compute and pair-compute



# NAMD kernel

## NAMD SPEC 2006 CPU benchmark kernel

- 1: for each atom  $i$  in patch  $p_k$
- 2:     for each atom  $j$  in patch  $p_i$ ,
- 3:         if atoms  $i$  and  $j$  are bonded, compute bonded forces
- 4:         otherwise, if atoms  $i$  and  $j$  are within the cutoff distance, add atom  $j$  to the  $i$ 's atom pair list
- 5:     end
- 6:     for each atom  $k$  in the  $i$ 's atom pair list
- 7:         compute non-bonded forces (L-J potential and PME direct sum, both via lookup tables)
- 8:     end
- 9: end

We implemented a simplified version of the kernel that **excludes pairlists and bonded forces**

- 1: for each atom  $i$  in patch  $p_k$
- 2:     for each atom  $j$  in patch  $p_i$ ,
- 3:         if atoms  $i$  and  $j$  are within the cutoff distance
- 4:             compute non-bonded forces (L-J potential and PME direct sum, both via lookup tables)
- 5:     end
- 6: end
-

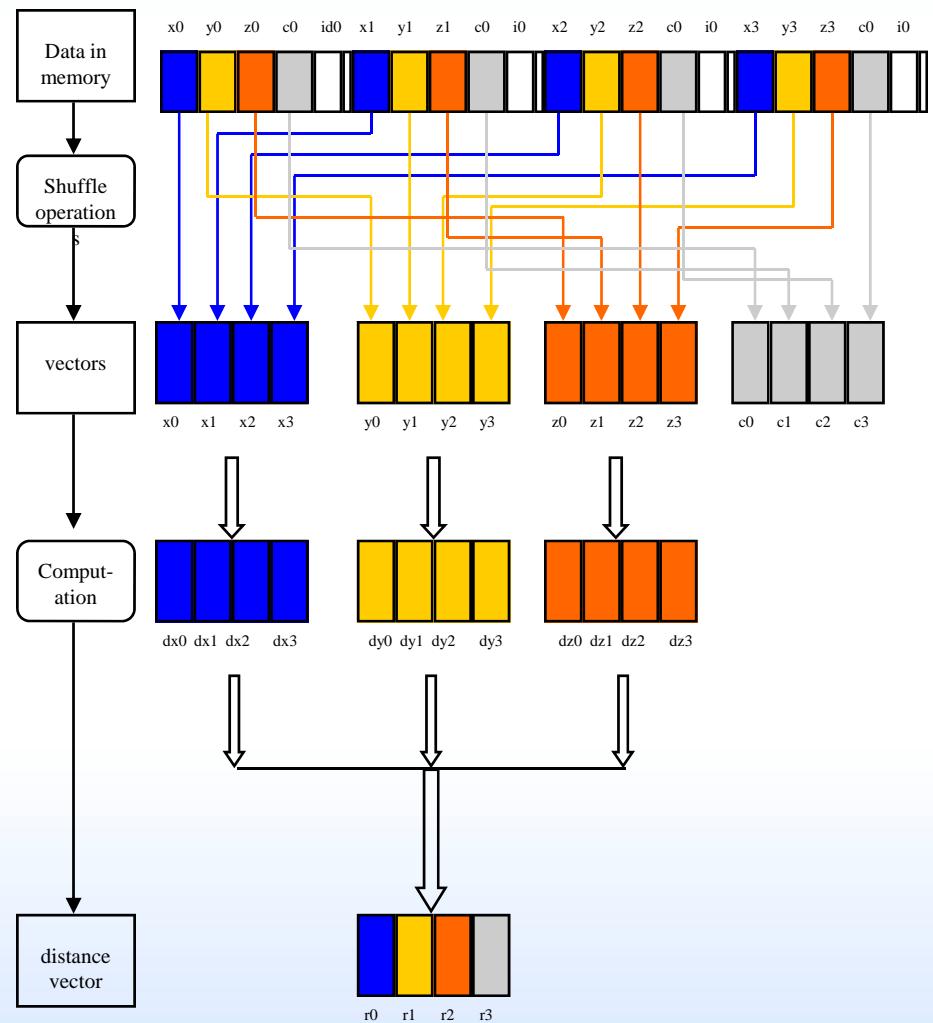
# NAMD Implementation: SPU

- SIMD: each component is kept in a separate vector
- Data movement dominates the time
- Buffer size carefully chosen to fit into the local store

**Local store usage**

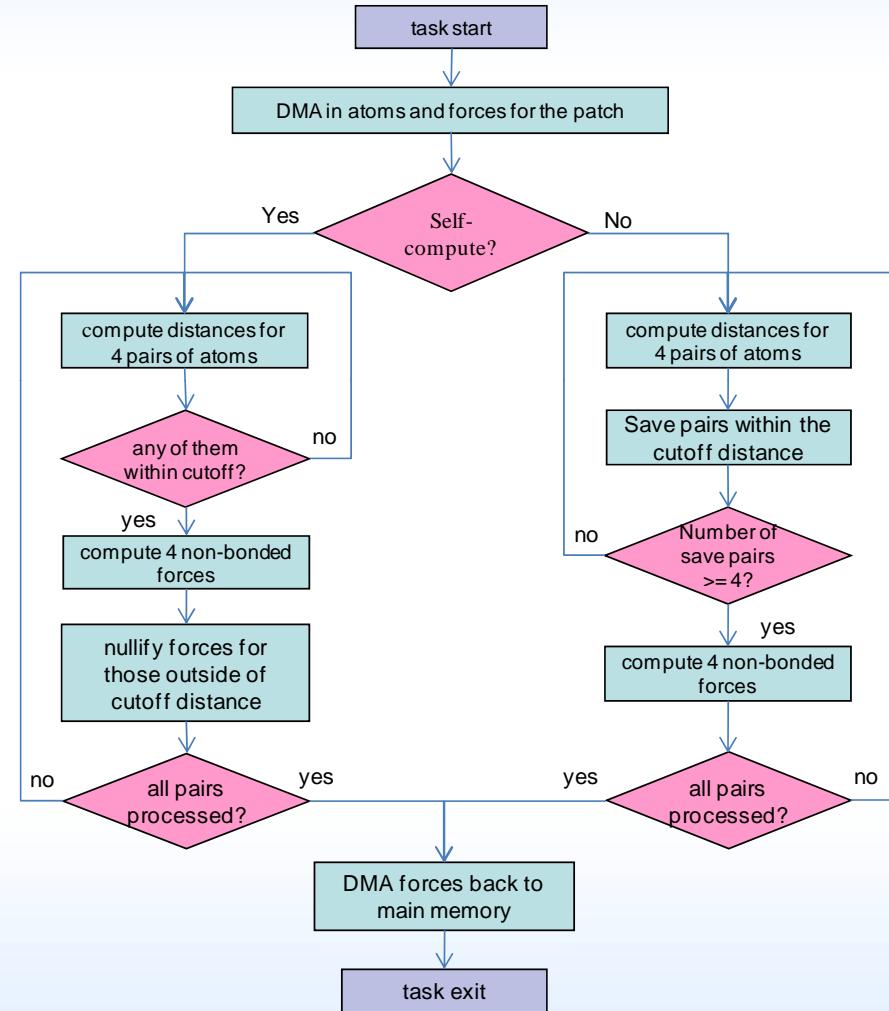
|    | Code<br>(KB) | L-J<br>table<br>(KB) | Table<br>_four<br>(KB) | Atom_<br>buffer<br>(KB) | Force<br>buffer<br>(KB) | Stack<br>others |
|----|--------------|----------------------|------------------------|-------------------------|-------------------------|-----------------|
| SP | 25           | 55                   | 45                     | 30                      | 18                      | 83              |
| DP | 25           | 55                   | 91                     | 48                      | 18                      | 19              |

**Data movement for distance  
computation (SP case)**

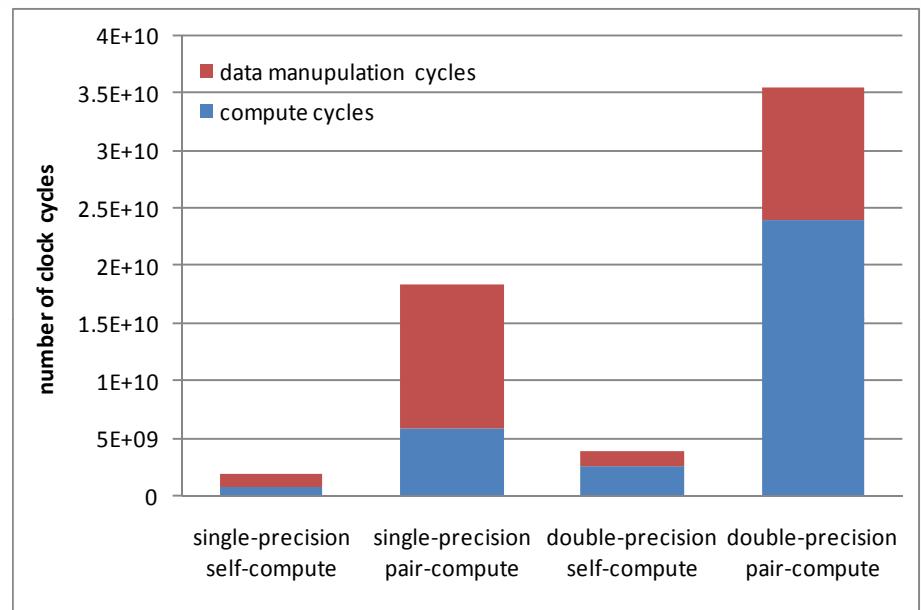
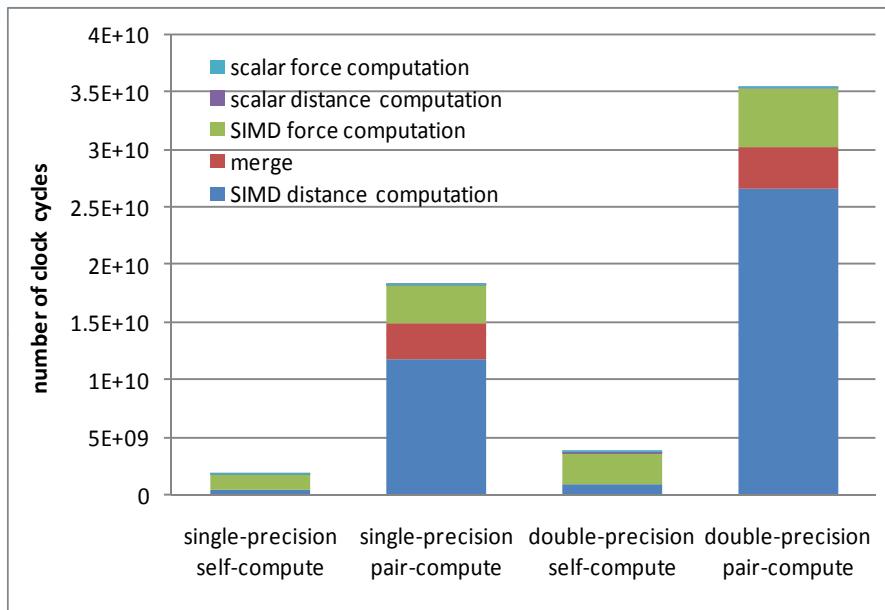


# Implementation: optimizations

- Different vectorization schemes are applied in order to get best performance
  - Self-compute: do redundant computations and fill zeros to unused slots
  - Pair-compute: save enough pairs of atoms, then do calculations



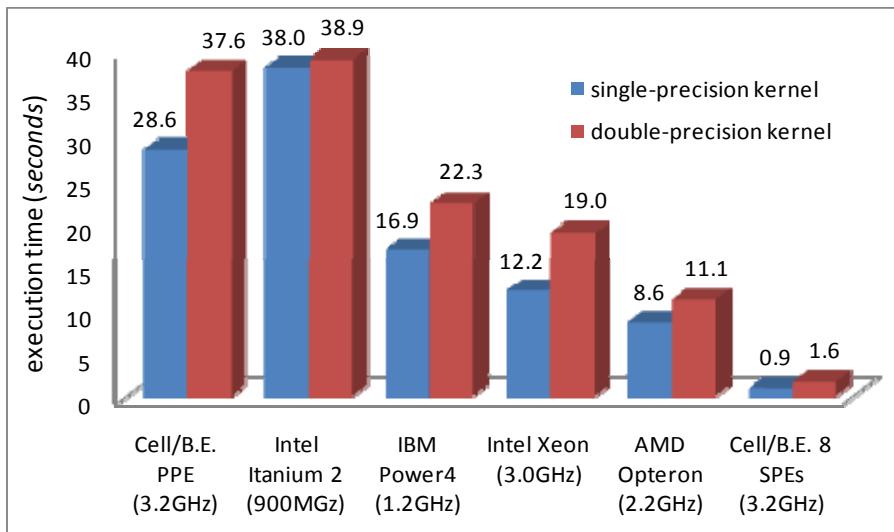
# NAMD Performance: static analysis



- Distance computation code takes most of the time
- Data manipulation time is significant

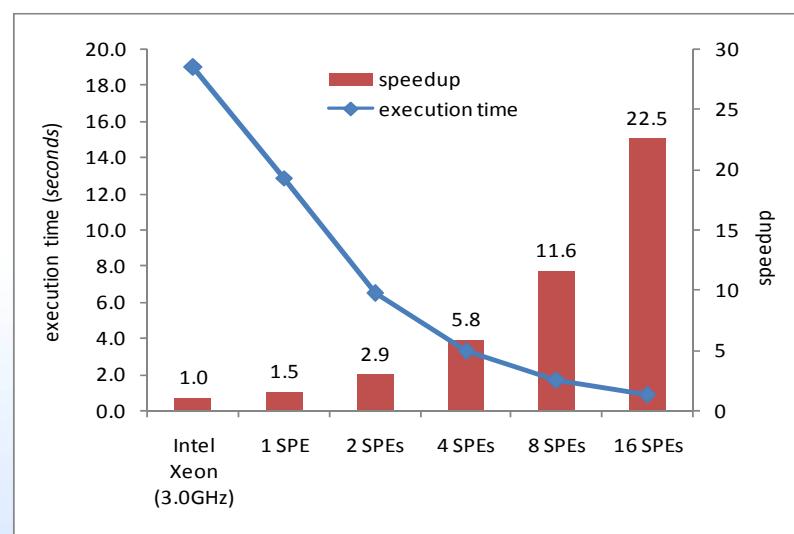
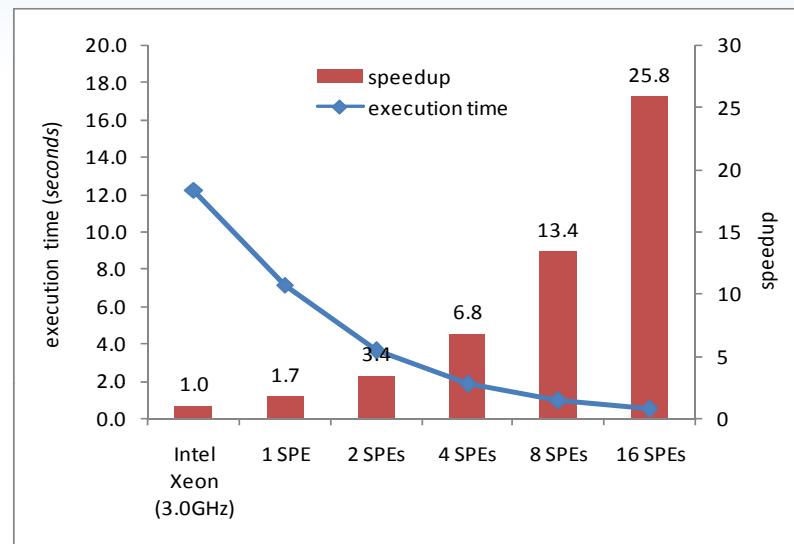
# NAMD Performance

## NAMD kernel performance on different architectures



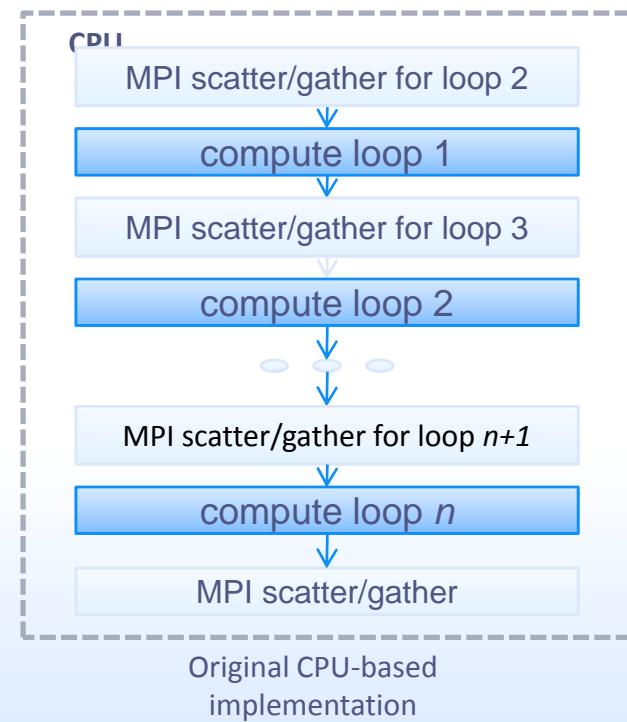
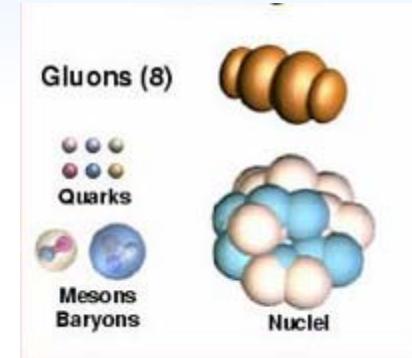
- 13.4x speedup for SP and 11.6x speedup for DP compared to a 3.0 GHz Intel Xeon processor
- SP performance is < 2x better than DP

## Scaling and speedup of the force-field kernel as compared to a 3.0 GHz Intel Xeon processor



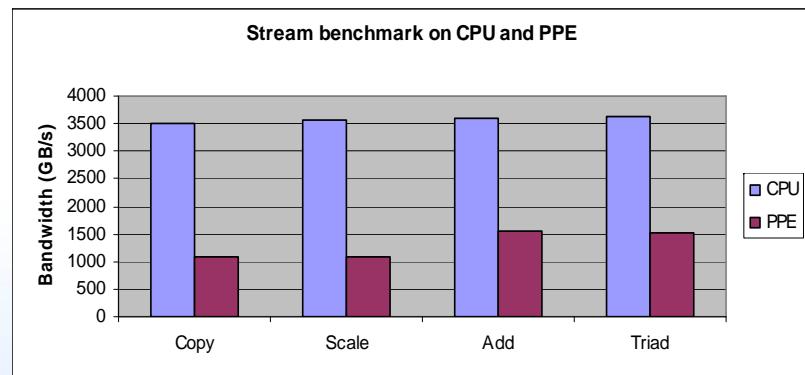
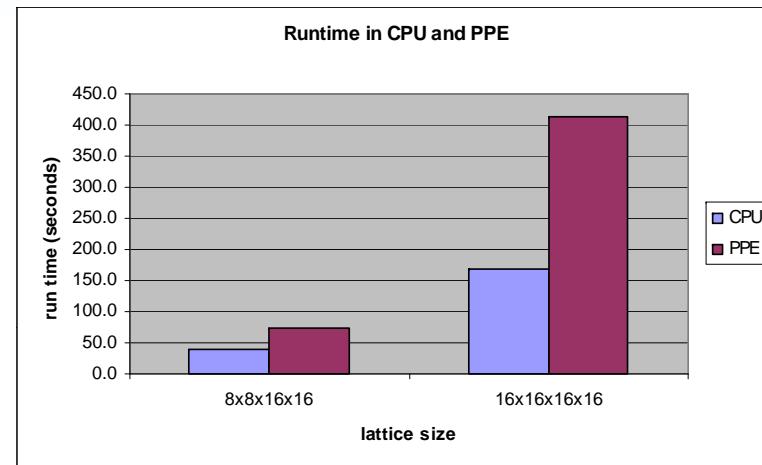
# MILC Introduction

- MILC studies large scale numerical simulations to study quantum chromodynamics (QCD), the theory of the strong interactions of subatomic physics.
- Large cycle consumer of supercomputers
- Our target application
  - dynamical clover fermions (`clover_dynamical`) using the hybrid-molecular dynamics  $R$  algorithm
- Our view of the MILC applications
  - A sequence of communication and computation blocks

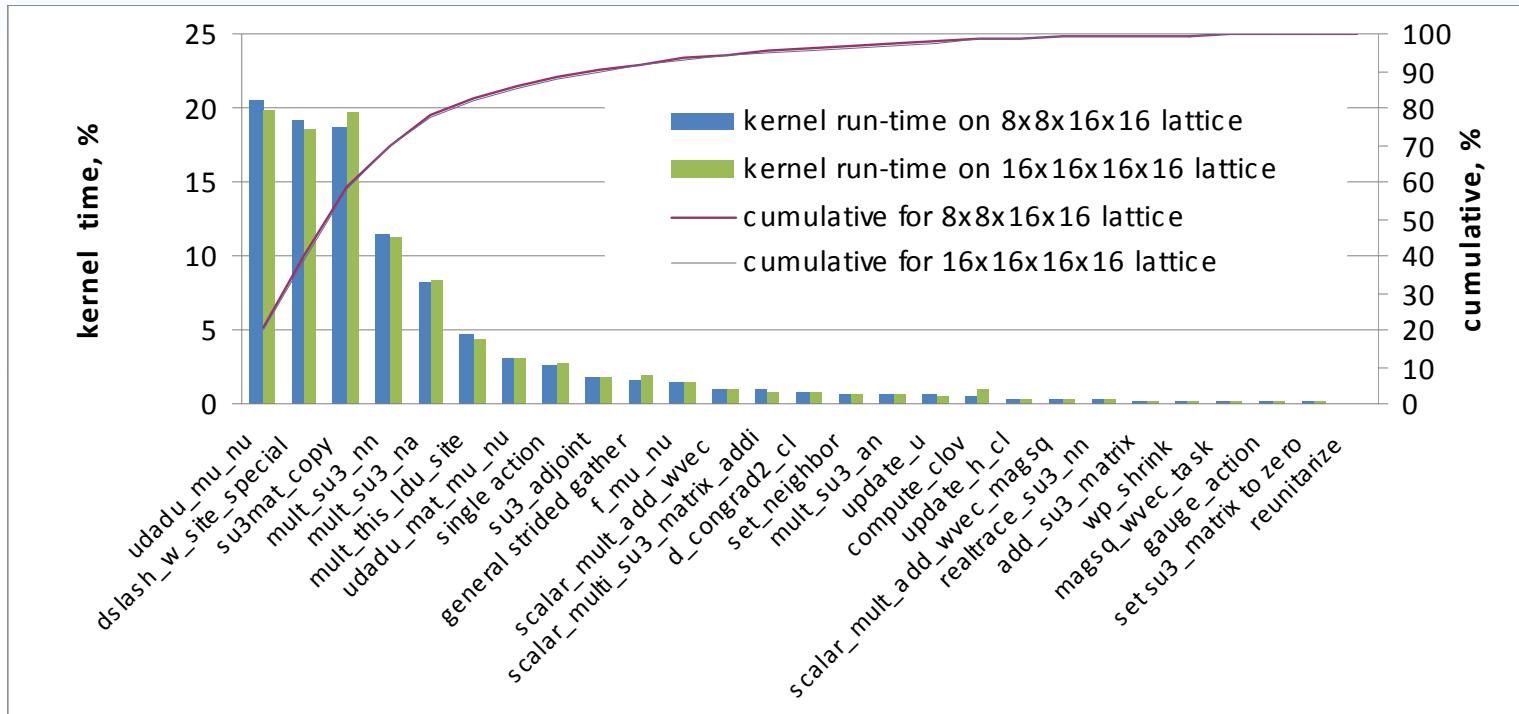


# MILC Performance in PPE

- Step 1: try to run it in PPE
- In PPE it runs approximately ~2-3x slower than modern CPU
- MILC is bandwidth-bound
- It agrees with what we see with stream benchmark



# MILC: Execution profile and kernels to be ported



- 10 of these subroutines are responsible for >90% of overall runtime
- su3mat\_copy, i.e. memcpy responsible for nearly 20% of all runtime
- All kernels responsible for 98.8%

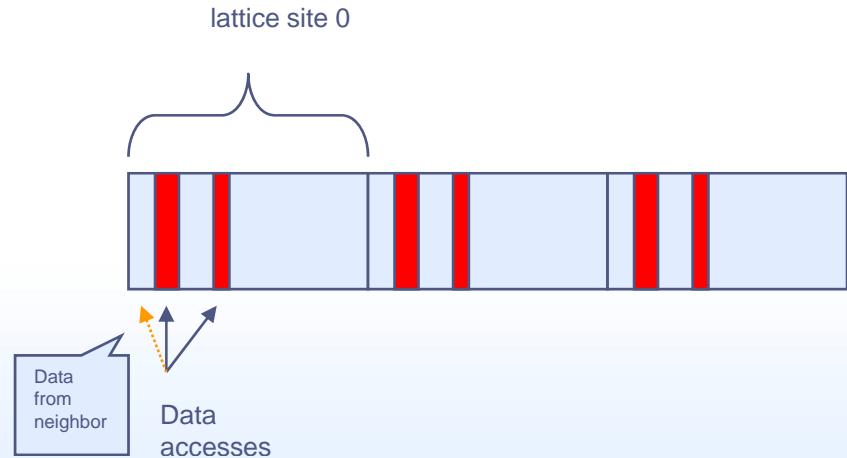
# MILC: Kernel memory access pattern

- Neighbor data access taken care of by MPI framework
- In each iteration, only small elements are accessed
  - Lattice size: 1832 bytes
  - su3\_matrix: 72 bytes
  - wilson\_vector: 96 bytes
- Challenge: how to get data into SPUs as fast as possible?
  - Data is nonaligned
  - Data is not multiple of 128 bytes

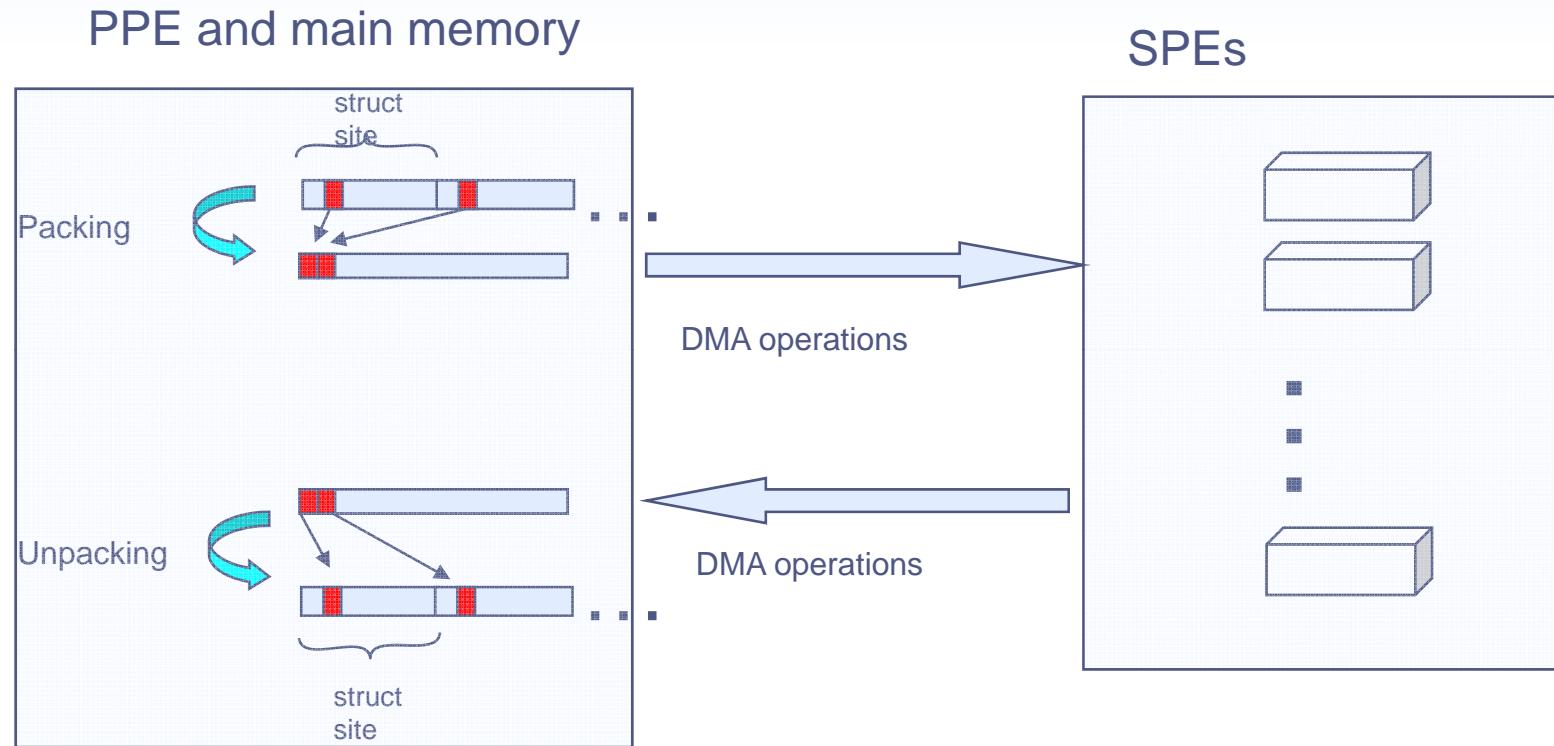
```
#define FORSOMEPRITY(i,s,choice) \
for( i==((choice)==ODD ? even_sites_on_node : 0 ), \
s= &(lattice[i]); \
i< ( (choice)==EVEN ? even_sites_on_node : sites_on_node); \
i++,s++)

FORSOMEPRITY(i,s,parity) {
    mult_adj_mat_wilson_vec( &(s->link[nu]), ((wilson_vector *)F_PT(s,rsrc)), &rtemp );
    mult_adj_mat_wilson_vec( (su3_matrix *) (gen_pt[1][i]), &rtemp, &(s->tmp) );
    mult_mat_wilson_vec( (su3_matrix *) (gen_pt[0][i]), &(s->tmp), &rtemp );
    mult_mat_wilson_vec( &(s->link[mu]), &rtemp, &(s->tmp) );
    mult_sigma_mu_nu( &(s->tmp), &rtemp, mu, nu );
    su3_projector_w( &rtemp, ((wilson_vector *)F_PT(s,lsrc)),
    ((su3_matrix*)F_PT(s,mat)) );
}
```

One sample kernel from *udadu\_mu\_nu()* routine

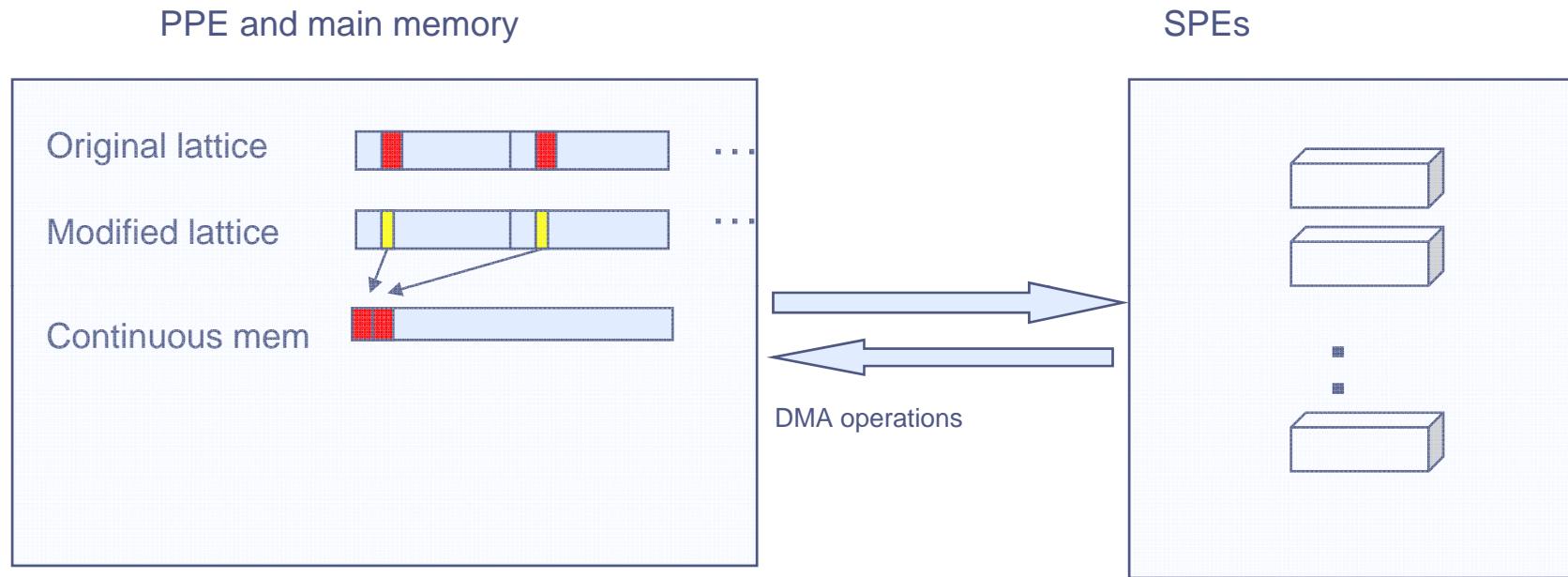


# Approach I: packing and unpacking



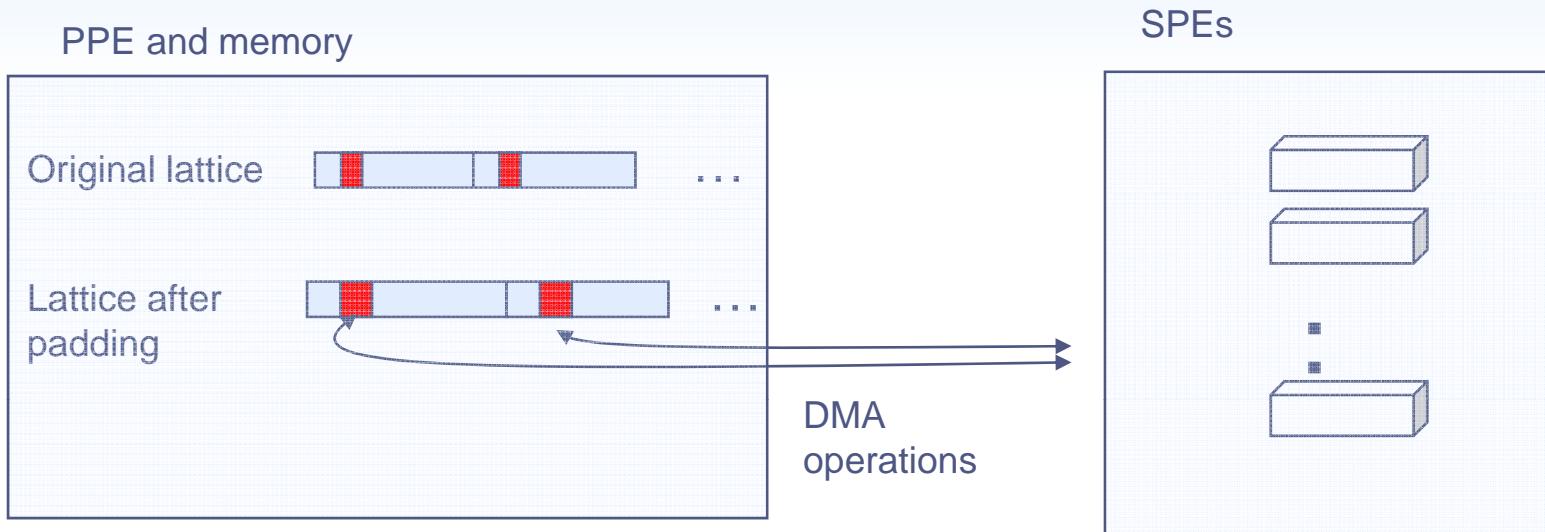
- Good performance in DMA operations
- Packing and unpacking are expensive in PPE

# Approach II: Indirect memory access



- Replace elements in struct site with pointers
- Pointers point to continuous memory regions
- PPU overhead due to indirect memory access

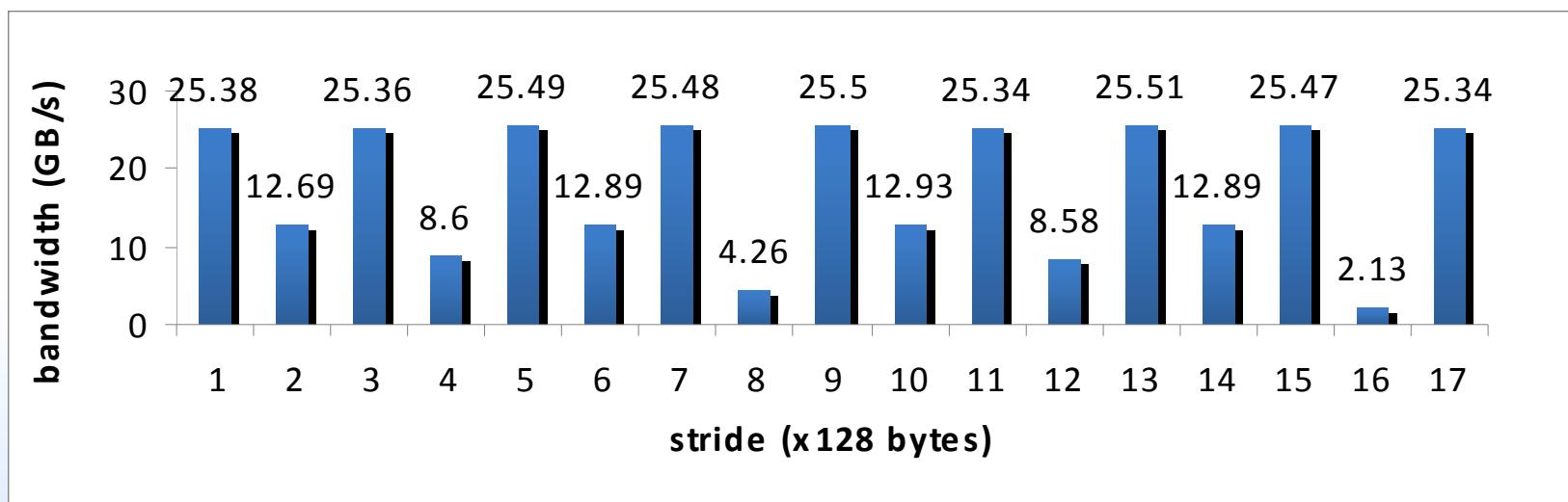
# Approach III: Padding and small memory DMAs



- Padding elements to appropriate size
- Padding struct size to appropriate size
- Gained good bandwidth performance with padding overhead
- Su3\_matrix from 3x3 complex to 4x4 complex matrix
  - 72 bytes → 128 bytes
  - Bandwidth efficiency lost: 44%
- Wilson\_vector from 4x3 complex to 4x4 complex
  - 98 bytes → 128 bytes
  - Bandwidth efficiency lost: 23%

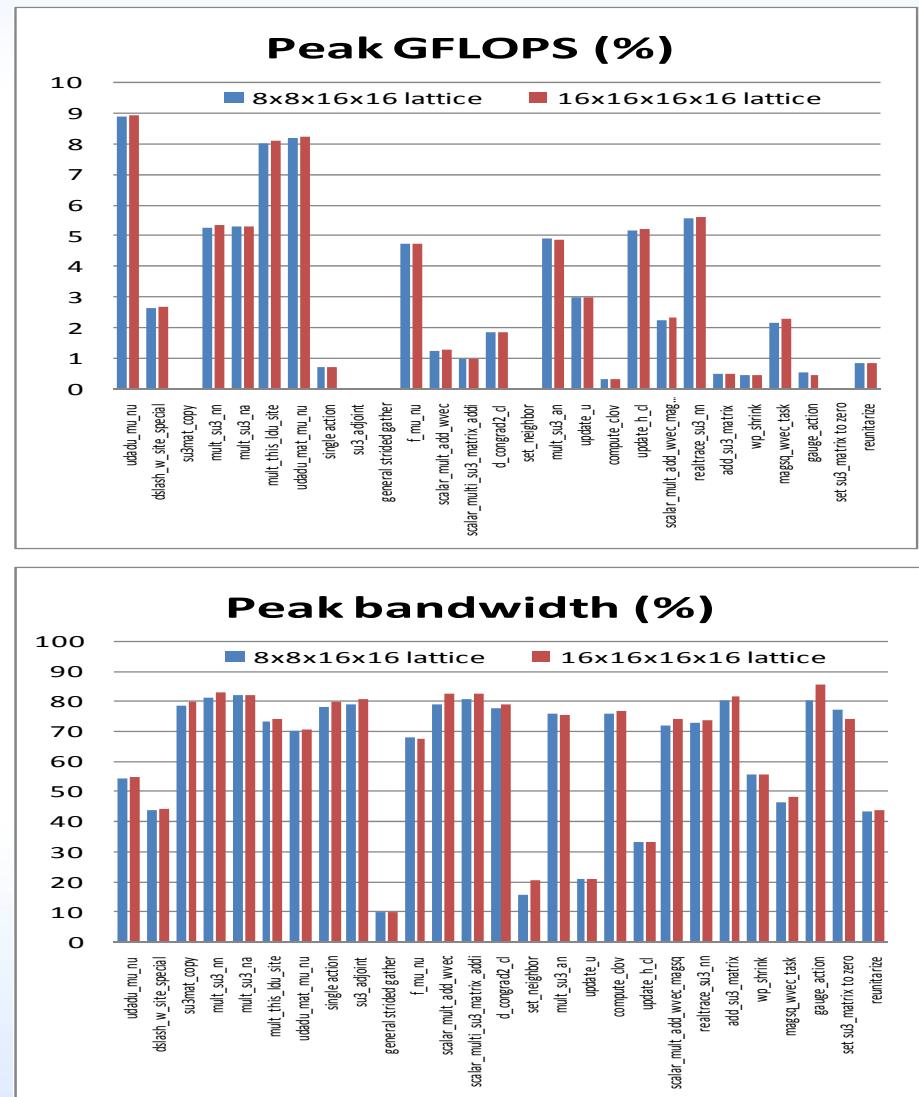
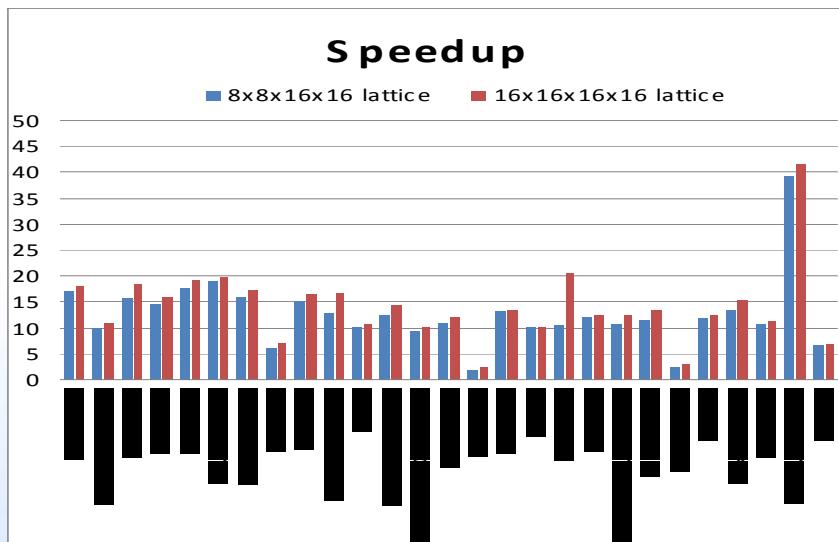
# MILC struct site padding

- 128 byte stride access has different performance
- This is due to 16 banks in main memory
- Odd numbers always reach peak
- We choose to pad the struct site to 2688 (21\*128) bytes



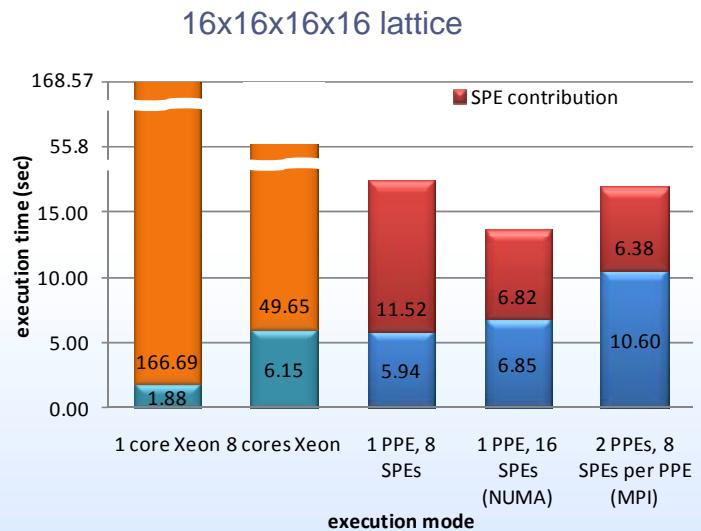
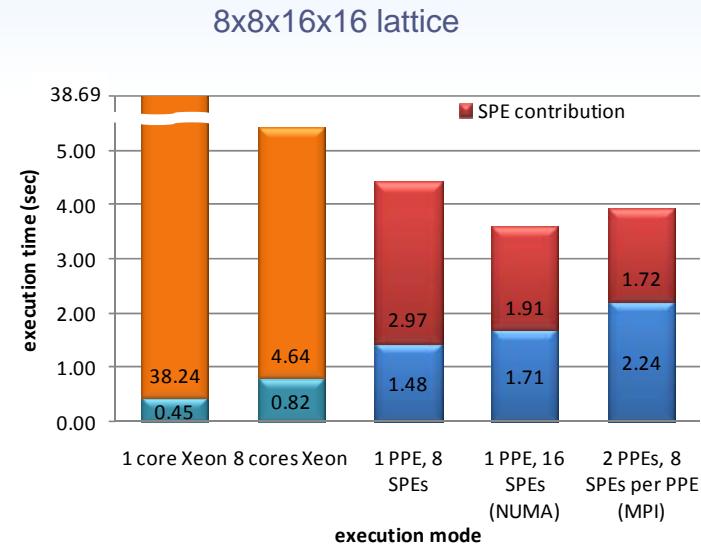
# MILC Kernel performance

- GFLOPS are low for all kernels
- Bandwidth is around 80% of peak for most of kernels
- Kernel speedup compared to CPU for most of kernels are between 10x to 20x
- set\_memory\_to\_zero kernel has ~40x speedup
- Memcpy speedup >15x



# MILC Application performance

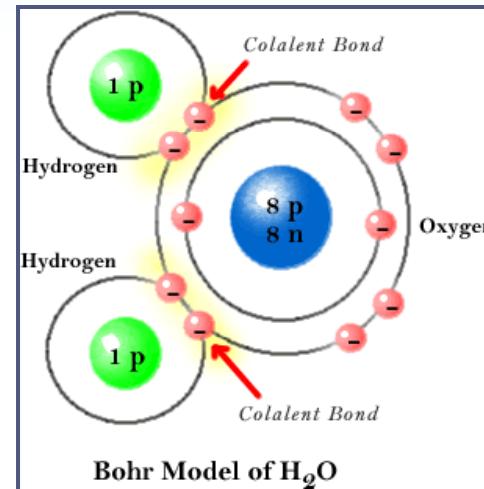
- Single Cell Application performance speedup
    - ~8–10x, compared to Xeon single core
  - Profile in Xeon
    - 98.8% parallel code, 1.2% serial code  
↓ speedup      ↓ slowdown
    - 67-38% kernel SPU time, 33-62% PPU time of overall runtime in Cell
- PPE is standing in the way for further improvement



# Introduction –Quantum Chemistry

- Two basic questions in Chemistry\* :
  1. Where are the electrons?
  2. Where are the nuclei?

→ Quantum Chemistry focuses the first question by solving the time-independent Schrödinger equation to get the electronic wave functions.  
And the absolute square is interpreted as the probability distribution for the positions of the electrons.
- The probability distribution function is usually expanded to Gaussian type basis functions.
- To find the coefficients in the above expansion, we need do lots of two electron repulsion integrals



$$\chi_{\mu}(\vec{r}) \propto (x - x_{\mu})^l (y - y_{\mu})^m (z - z_{\mu})^n \exp(-\alpha_{\mu} |\vec{r} - \vec{R}_{\mu}|^2)$$

Gaussian type basis functions

$$(\mu\nu | \lambda\sigma) = \iint \frac{\chi_{\mu}(\vec{r}_1)\chi_{\nu}(\vec{r}_1)\chi_{\lambda}(\vec{r}_2)\chi_{\sigma}(\vec{r}_2)}{|\vec{r}_1 - \vec{r}_2|} d\vec{r}_1 d\vec{r}_2$$

two Electron Repulsion Integral (ERI)

\* <http://mtzweb.scs.uiuc.edu/research/gpu/>

# Introduction – Electron Repulsion Integral (ERI)

Reference CPU implementation

```

for (s1 = startShell; s1 < stopShell; s1++)
    for (s2 = s1; s2 < totNumShells; s2++)
        for(s3 = s1; s3 < totNumShells; s3++)
            for(s4=s3; s4 < totNumshells; s4++)

            for (p1=0;p1< numPrimitives[s1]; p1++)
                for (p2=0;p2< numPrimitives[s2]; p2++)
                    for (p3=0;p3< numPrimitives[s3]; p3++)
                        for (p4=0;p4< numPrimitives[s4]; p4++)
                        {

                            .....

                            H_ReductionSum[s1,s2,s3,s4 += sqrt(F_PI*rho)*
                                I1*I2*I3*Weight*Coeff1*Coeff2*Coeff3*Coeff4;
                        }

```

$$(\mu\nu|\lambda\sigma) = \sum_{p=1}^{N_\mu} \sum_{q=1}^{N_\nu} \sum_{r=1}^{N_\lambda} \sum_{s=1}^{N_\sigma} d_{\mu p} d_{\nu q} d_{\lambda r} d_{\sigma s} [pq|rs]$$

The general form for [ss|ss] integral

$$[s_1 s_2 | s_3 s_4] = \frac{\pi^3}{AB\sqrt{A+B}} K_{12}(\vec{R}_{12}) K_{34}(\vec{R}_{34}) F_0\left(\frac{AB}{A+B} [\vec{R}_P - \vec{R}_Q]^2\right)$$

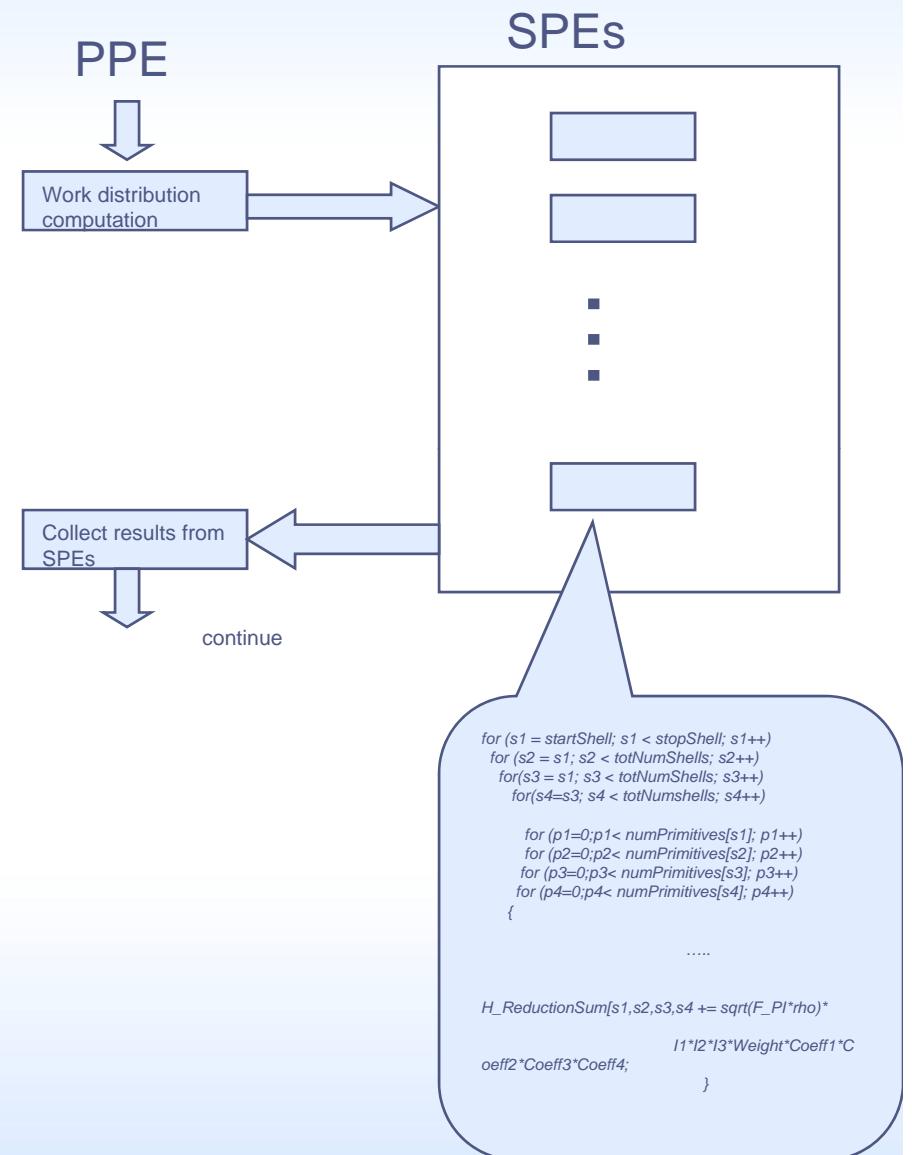
where

$$\begin{aligned}
 A &= \alpha_1 + \alpha_2, \quad B = \alpha_3 + \alpha_4, \quad F_0(t) = \frac{\text{erf}(\sqrt{t})}{\sqrt{t}}, \\
 \vec{R}_{kl} &= \vec{R}_k - \vec{R}_l, \quad \vec{R}_P = \frac{\alpha_1 \vec{R}_1 + \alpha_2 \vec{R}_2}{A}, \quad \vec{R}_Q = \frac{\alpha_3 \vec{R}_3 + \alpha_4 \vec{R}_4}{B}, \\
 K_{ij}(\vec{R}_{ij}) &= \exp\left(-\frac{\alpha_i \alpha_j}{\alpha_i + \alpha_j} [\vec{R}_i - \vec{R}_j]^2\right)
 \end{aligned}$$

- Four outer loops sequence through all unique combinations of electron shells
- Four Inner loops sequence through all shell primitives
- The primitives [ss|ss] are computed and summed up in the core code.

# Porting to Cell B.E. – load balance

- Function offload programming
- Each SPE is assigned a range of (s1,s2,s3,s4) to work on.
- Load balance Computation in PPE
  - Each primitive integral roughly has the same amount of computation
  - Each contracted integral may have different amount of computation
  - Each iteration in outer most loop has different amount of computation
  - PPE must compute the amount of computation before SPEs run



# SPE kernels

- Is local store enough:
  - Input data: an array of coordinates + an array of shells + an array of primitives < 32 KB
  - The Gauss error function -- erf() – is evaluated by interpolating table. The table size is < 85KB
  - We have enough local store
- Precomputing is necessary to reduce redundant computation
  - Precomputed intermediate results are much larger than local store

# SPE kernel -- precompute

- Instead of computing every primitive integrals from equations, we precompute pairwise quantities and store them in main memory
- DMA all pairwise quantities before computing a contracted integral
- Precomputed quantities:

$$\alpha_1 + \alpha_2$$

$$d_1 d_2 \left( \frac{\pi}{\alpha_1 + \alpha_2} \right)^{3/2} e^{-\alpha_1 \alpha_2 / (\alpha_1 + \alpha_2) \vec{R}_{12}^2}$$

$$(\alpha_1 \vec{R}_1 + \alpha_2 \vec{R}_2) / (\alpha_1 + \alpha_2)$$

- Trade bandwidth with computation

```
for (s1 = startShell; s1 < stopShell; s1++)  
  for (s2 = s1; s2 < totNumShells; s2++)  
    for(s3 = s1; s3 < totNumShells; s3++)  
      for(s4=s3; s4 < totNumshells; s4++)
```

*DMA in precomputed pair quantities.*

```
for (p1=0;p1< numPrimitives[s1]; p1++)  
  for (p2=0;p2< numPrimitives[s2]; p2++)  
    for (p3=0;p3< numPrimitives[s3]; p3++)  
      for (p4=0;p4< numPrimitives[s4]; p4++)  
      {  
        .....  
        H_ReductionSum[s1,s2,s3,s4 += sqrt(F_Pl*rho)*  
                      I1*I2*I3*Weight*Coeff1*Coeff2*Coeff3*Coeff4;  
      }
```

# SPE kernel – inner loops optimizations

- Naïve way of SIMDing kernel
  - Use a counter to keep track of the number of primitive integrals
  - If counter  $\geq 4$ , do a 4-way computation
- Loop switch
  - If one of the loops' length is multiple of 4, we switch the loop to the inner most
  - Advance in increment of 4, and get rid of counter
- Loop unrolling
  - If the numPrimitives are the same for all primitive integral and the happened to be some nice number
  - Completely unroll the inner loops generate the most efficient code

```
for (p1=0;p1< numPrimitives[s1]; p1++)
    for (p2=0;p2< numPrimitives[s2]; p2++)
        for (p3=0;p3< numPrimitives[s3]; p3++)
            for (p4=0;p4< numPrimitives[s4]; p4++)
{
    static int count =0;
    count++;
    if (count == 4){
        compute 4 primitive integrals using SIMD intrinsics
    }
}
```

Naïve implementation of SIMD kernel

.....  
DMA in precomputed pair quantities.

```
for (p4=0;p4< numPrimitives[s4]; p4++)
    for (p2=0;p2< numPrimitives[s2]; p2++)
        for (p3=0;p3< numPrimitives[s3]; p3++)
            for (p1=0;p1< numPrimitives[s1]; p1+=4)
{
    Compute 4 primitive integrals in SIMD intrinsics
}
```



Loop switch: loop1 length is multiples of 4, switch loop1 and loop4

# Performance results

|                         | Model1      | Model2        |
|-------------------------|-------------|---------------|
| # of Atoms              | 30          | 64            |
| Basis set               | 6-311G      | STO-6G        |
| # of integrals          | 528,569,315 | 2,861,464,320 |
| # of reduction elements | 3,146,010   | 2,207,920     |
| Xeon (2.33Ghz)          | 21.04       | 112.55        |
| Cell-blade (16 SPEs)    | 1.1         | 0.92          |
| Speedup                 | 19x         | 122x.         |

- Model1 is 10 water molecules (30 atoms in total), model2 is 64 hydrogen atom arranged in lattice
- Model1 has non-uniform contracted integral intensity, ranging from 4096 to just 1 primitive integrals.
  - Loop switching is not always possible → naïve SIMD implementation → more control overhead
  - Loop unrolling is not possible since the # of iterations in each inner loop changes
  - Precomputing proves to slow down due to DMA overhead
- Model2 uniform computation intensity
  - Precomputing and loop unrolling proves to be efficient
  - Module outperforms GPU implementation\*

\* Quantum Chemistry on Graphical Processing Units. 1. Strategies for Two-Electron Integral Evaluation. Ivan S. Ufimtsev and Todd J. Martinez, Journal of Chemical Theory and Computation, February 2008

# Summary

|      | Ported code     | Precision | Performance Limit factor | Cell Blade to single core speedup <sup>1</sup> | Cell blade to Xeon blade speedup <sup>2</sup> |
|------|-----------------|-----------|--------------------------|--|---|
| NAMD | Modified kernel | SP,DP     | Computation              | 22-26x   | NULL  |
| MILC | application     | SP        | Bandwidth                | 10-12x   | 1.5-4.1x                                      |
| ERI  | Kernel          | SP        | Computation              | 19-122x  | NULL  |

1. CPU comparing core for NAMD 3.0Ghz Xeon, for MILC and ERI it is 2.33 Ghz Xeon
2. One Xeon blade contains 8 cores with 2MB L2 cache per core.

# Lessons learned

- Keep code on PPE to a minimum
  - 1.2% runtime code → 33-62% in PPE in MILC
- Find out the limiting factor in the kernel and work on it
  - MILC is bandwidth limited and we focus on improving the usable bandwidth
  - NAMD and ERI is compute-bound and we focus on optimizing the SIMD kernel.
- Sometimes we can trade bandwidth with computation or vice versa
  - In ERI, depends on input data, we can either precompute some quantities in PPE and DMA in or do all computation in SPEs
- Application data layout in memory is critical
  - Padding would not be necessary if MILC is field centered → improvement of performance and productivity
  - Proper data layout makes SIMDizing kernel code easier and make it faster

# Thank You

- Questions?